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INTRODUCTION

Insurance	A financial arrangement in which participants make payments in exchange for a commitment to indemnify certain types of losses.
Reinsurance	An arrangement where insurer transfers away a part of the risk to another company (known as reinsurer).
Written Premium	The total amount of premium received from policies for which cover commenced during a specific accounting period.
Earned Premium	The portion of written premium for which coverage has already been provided during a specific accounting period.
Unearned Premium	The portion of written premium for which coverage has not yet been provided and is deemed to relate to cover in one or more subsequent accounting periods.
Incurred Claims	The total of all claims paid plus the total reserves for outstanding reported claims (the total reserves for outstanding claims are also called case estimates).
Claims Handling Expenses	The expenses incurred in handling and settling claims. Also known as 'loss adjustment expenses' in the US.
Written Exposure	The total exposure that arises during a period.
Earned Exposure	The portion of written exposure for which coverage has already been provided.
Technical Reserves	The reserves held to cover the liabilities relating to insurance policies already writ- ten.
Reserves for Outstanding Reported Claims	The estimated reserves needed to settle all the claims reported to the insurer at an accounting date.
IBNR Reserve	The estimated amount that is needed to cover the claims for which accident events have happened but not yet reported to the insurer at an accounting date.
IBNER Reserve	The estimated amount that is needed to cover the changes in estimates of reported claims as at an accounting date.
Unearned Premium Reserve	A retrospective reserve held for premiums that have not been earned yet as at an accounting date.
Unexpired Risk Reserve	A prospective reserve required to cover the claims and claims handling expenses expected to emerge from an unexpired period of cover.
Claims Equalisation Reserves	A reserve maintained to smooth out fluctuations in claims experience over time.
Free Reserves	The excess of the value of assets of an insurer over the sum of its technical provisions and current liabilities.
Reporting Delay	The time gap between occurrence of a claim event and reporting the same to the insurer.
Settlement Delay	The time gap between reporting of a claim to the insurer and its settlement to the insured.

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Short-tail line	A line of business where claims are generally reported and settled quickly.
Long-tail line	A line of business where claims take time (years, or even decades) to be reported, assessed, and settled.
Underwriting Income	The income earned by the insurer from its core insurance operations, also known as operating income.
Investment Income	The income earned by the insurer from its investment portfolio.
Accident Year	An aggregation method where only the loss transactions relating to the loss events that occurred during that period are grouped together.
Calendar Year	An aggregation method where all premiums and loss transactions that occur during a twelve-month period are grouped together.
Underwriting Year	An aggregation method where all premiums and loss transactions on policies written during that period are grouped together.
Reporting Year	An aggregation method where only the loss transactions relating to the loss events that are reported during that period are grouped together.

GENERAL INSURANCE PRODUCTS

Uberrima Fides	Principle of utmost good faith observed by parties of insurance contract.
Suretyship	Insurance to provide for the financial obligations of the insured, if the insured fails to do so.
Underinsurance	A situation when the sum insured is lower than the value of contents specified in insurance contract.
Discovery Period	A time limit within which claims must be reported to the insurer.
Deductible	An amount that the insured must pay before the insurer starts to pay.
Excess	Similar to deductibles, but does not reduce the maximum payout.
Salvage	Amount recovered from sale of insured items that become property of insurer after settling the claim.
Subrogation	An insurer, after paying claims, assumes insured's legal rights to recover the amount from a third party.
Recoveries	Amount recovered to offset the cost of claims, including salvage, subrogation, rein- surance recoveries, etc.
Lapse	A policy that, when invited to renew, does not do so.
Cancellation	A cessation of the policy, which may involve a partial return of premiums.
Underwriting	A process of assessing whether the risk is acceptable and, if so, determining the appropriate premium with the terms and conditions of the cover.
Claim Frequency	The number of claims in a period per unit of exposure.
Claim Severity	Average claim amount
Claims Made Policy	A policy that covers all claims reported to an insurer within the policy period, irrespective of when the loss occurred.
Losses Occurring Policy	A policy that covers all losses that occurred within the policy period, irrespective of when the loss is reported.

	SP8 Summary Sheet 3
Risk Attaching Policy	A basis under which reinsurance is provided for claims arising from policies com- mencing during the period to which the reinsurance relates.
Latent Claims	Claims that result from perils that the insurer is unaware of at the time of writing a policy.
Probable Maximum Loss	Estimated largest loss expected to arise from a single event in respect of an insured property.
Criteria for Insurable Risk	 Criteria for a risk to be insurable: Interest in the risk being insured Risk must be financial and of a quantifiable nature Claim amount having a relationship with the financial loss incurred Risk events to be independent of each other Probability of the event occurring is very small A large number of similar risks to be pooled to reduce variance There must be an overall limit on the risk taken Moral hazards to be eliminated as much as possible Need for sufficient data to price risks
Policy Document	This sets out the terms and conditions under which the insurer is liable to pay claims. Items might include details of cover, excess, exclusions, details of premiums, etc.
Exclusion	Exclusions are clauses that limit the circumstances in which a claim may be made. Examples include losses caused by terrorism, depreciation to a motor vehicle, etc.
Claim Characteristics	This refers to ways in which, and the speed with which, claims originate, are notified, settled, paid, and reopened. They are defined by frequency, severity claims inflation, delay pattern, accumulation of risk, and fraudulent claims.
Rating Factors	Risk factor is any characteristic or measure that has an influence on the likelihood or severity of a claim. Rating factors are the proxies of risk factors used in pricing.
Exposure Measure	Measures that are used to quantify the level of risk underlying an insurance coverage. Examples include sum insured, vehicle-years, etc.
Capital Requirements	The amount of capital held is subject to minimum requirements if a company is to be allowed to continue to trade.
Lines of Business	 There are four main types of GI (General Insurance) Covers under which products are sub categorized. They are: Liability Insurance Property Insurance Financial Loss Insurance Fixed Benefits Insurance
Employer's Liability	This indemnifies the insured against legal liability for employee injury, disease, or death due to negligence during employment. The basis of cover is a loss-occurring basis . The exposure measure used is payroll . The rating factors used are type of occupation, workforce location, claims experience, site visitors, and materials handled.
Motor Third Party	This covers the insured's liability for third-party injury or property damage caused by their vehicle. The basis of cover is a loss-occurring basis. The exposure measure used is vehicle-years . The rating factors used are driver experience , vehicle make/model , safety features , and location .

Marine and Aviation Liability	This covers the insured's liability for third-party injury, death, or property damage arising from operating a vessel or aircraft. The basis of cover is a loss-occurring basis. The exposure measures used are passenger kilometers , voyages, or in- service capacity. The rating factors used are loss experience, craft type, operating region, usage, and commercial category.
Public Liability	This indemnifies the insured against liability for third-party injury or property damage not covered by other liability insurance. The basis of cover is either a loss-occurring or claims-made basis. The exposure measure is turnover . The rating factors used depend on the policy type and coverages offered.
Product Liability	This covers the insured's liability for third-party injury or property damage due to product faults. The basis of cover is a claims-made basis. The exposure measure used is turnover . The rating factors include distribution channel , product type , usage , and sales/manufacturing region .
Professional Indemnity	This covers the insured's liability for client losses due to negligence in professional services. The basis of cover is a claims-made basis. The exposure measure used is turnover . The key rating factors include service type , firm size, and professional experience.
Director's and Officer's Liability	This covers legal liability for wrongful acts committed by directors/officers, such as trading while insolvent or publishing false financial statements. It operates on a claims-made basis, with turnover as the exposure measure. The key rating factors include company nature and directors' experience .
Pollution Liability	This covers liability for unintentional pollution. It operates on a claims-made basis, with the exposure depending on the industry type. The key rating factors include business processes , potential accident impact , and cleanup costs .
Residential/Commercial Buildings	This policy covers damage to residential/commercial property from fire, theft, and other perils, paying for restoration costs minus any deductible. The basis of cover is a loss-occurring basis. The exposure measure is sum insured-years . Key factors include sum insured, location, property use, and building age .
Moveable Property	This policy covers loss or damage to household contents due to fire, theft, or other perils, often as an extension of home insurance. Claims may be paid on a replacement value or new-for-old basis. It follows a loss-occurring basis. The exposure measure is sum insured-years . The risk factors are similar to those for residential property insurance.
Motor Property	This policy covers third-party vehicle damage and losses to the insured's own vehicle due to fire, theft, or accidental damage. The basis of cover is loss-occurring basis. The exposure measure is vehicle-years . The key rating factors include mileage , traffic density, driver skill, speed, vehicle durability, and theft risk .
Marine and Aircraft	This policy covers loss or damage to aircraft, ships, or their contents, as defined in the Marine Insurance Act. The basis of cover is loss-occurring basis. The exposure measure is sum-insured . Key factors include craft size , type , age , and the nature of the cargo .
Goods in Transit	This policy covers loss or damage to goods in transit due to theft, damage, or other perils. The basis of cover is loss-occurring basis. The exposure measure is consignment value . Key factors include transport mode , goods type, storage, transit duration, and warehouse time.

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Construction	This policy covers large construction and engineering projects, including dama defects, or failure to complete. The basis of cover is a loss-occurring basis. The exposure measure is contract value . Key factors include project type , duratic contractor , materials , technology , and location .	The
Extended Warranty	This policy covers repair or replacement costs for faulty parts beyond the manu turer's warranty, usually for electronics, furniture, or vehicles. The basis of co is a loss-occurring basis. The exposure measure is appliance-years . Key tors include item make/model , manufacturer's warranty length , and pol term .	over fac-
Fidelity Guarantee	This policy covers financial losses from employee dishonesty, such as fraud or bezzlement. It follows a loss-occurring basis, with the exposure measured as loan amount exceeding a set percentage of the property value.	
Credit Insurance	This policy covers losses when debtors fail to meet their financial obligations. includes trade credit and mortgage indemnity insurance. The basis of cover loss-occurring basis. The exposure measure is the loan amount exceeding a percentage of the property's value.	is a
Creditor Insurance	This policy covers individuals who are unable to meet financial obligations due disability or unemployment. The basis of cover is a loss-occurring basis. The exposure measure is loan amount . Covered risks typically include accidents, abilities, or job loss leading to income loss.	The
Business Interruption Cover	This policy compensates businesses for financial losses incurred due to their ina ity to operate, typically caused by fire at their premises or nearby properties. operates on a loss-occurring basis, with turnover as the measure of exposure	s. It
Legal Expense Cover	This insurance covers the insured for legal expenses arising from legal proceeding against them. The basis of cover is either a loss-occurring or claims-ma basis . The measure of exposure is policyholder-years .	-
Personal Accident	This insurance pays fixed benefits if the insured (or their family) suffers accident death or a specified injury, such as losing a limb. It operates on a loss-occurr basis, with sum insured as the measure of exposure. The key rating factors incl age, gender, and hazardous hobbies.	ring

REINSURANCE PRODUCTS

Retrocession	Reinsurance of reinsurance	
Inward Reinsurance	Reinsurance business accepted or written by a reinsurer	
Outward Reinsurance	Reinsurance business ceded by an insurer	
Participants in Reinsurance Markets	Participants in reinsurance market include: 1. brokers 3. fronting 2. direct reinsurance placements 4. captives	
Fronting	Fronting occurs when an insurer, acting as a mere conduit, underwrites a risk and cedes all (or nearly all) of the risk to another insurer which is technically acting as a reinsurer.	
Captives	An entity set up with the primary purpose of insuring the risks of its parent company or associated group companies.	
Reinstatement	The restoration of full cover following a claim	

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Overriding Commission	Additional commission paid by a reinsurer to an insurer ceding proportional busi- ness, as a contribution towards expenses and profit.	
Profit Commission	A commission paid by the reinsurer to the insurer as a reward for underwriting a profitable business.	
Reasons for purchasing Reinsurance	 Common reasons for purchasing reinsurance include: 1. Limitation of exposure to risk or spreading of risk 2. Avoidance of large single losses 3. Smoothing of results 4. Increasing profitability 5. Improving solvency margins 6. Increasing capacity to accept risk 7. Financial assistance to insurers 8. Availability of expertise of reinsurers 	
Factors affecting Insurer's risk appetite	An insurer's risk appetite is influenced by its size, experience in the marketplace, available free assets, size of portfolio, and range within which business outcome may be forecast with confidence.	
Ways of writing Reinsurance	Reinsurance may be written on a facultative or treaty basis.	
Facultative Reinsurance	Reinsurance of a single risk. Each risk on which reinsurance is required is offered separately.	
	$\underline{\text{Advantages}}$ – flexibility, mitigation of accumulation of risk, and selective coverage	
	Disadvantages – time consuming, costly, no certainty, unacceptable terms, insurer cannot accept business automatically when offered. A facultative reinsur- ance facility with an obligation placed on the reinsurer to accept is known as facultative-obligatory reinsurance	
Treaty Reinsurance	Reinsurance of a group of similar risks under one reinsurance arrangement. It overcomes all disadvantages of facultative reinsurance.	
Proportional Reinsurance	A reinsurance arrangement where the reinsurer and the cedant share claims and premiums proportionally. Types include Quota Share , and Surplus Lines .	
Non-proportional Reinsurance	A reinsurance arrangement where the reinsurer and the cedant do not share claims and premiums proportionally. Types include Excess of Loss and Stop Loss Reinsurance .	
Quota Share Reinsurance	Insurer and reinsurer share the same proportion of premiums and losses for all risks covered under the treaty. The cedant's loss ratio for the account will be the same before and after reinsurance. The reinsurer would experience a similar claim experience as the cedant due to the proportional share of claims.	
	$\underline{\text{Advantages}}$ – spreads risk, improves solvency ratio, and is easy to administer	
	$\underline{\text{Disadvantanges}} - \text{cedes the same proportion of low-variance/high-variance risk,} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	
Surplus Lines Reinsurance	The insurer decides the proportion of premiums and losses to be shared individually for each risk, subject to limits defined in the treaty. The insurer and reinsurer would have different claim experiences.	
	$\underline{\text{Advantages}}$ – enables writing of large risks, spreads risk, useful when there is a wide variation in the size of risk, and enables the insurer to choose which risk to retain	

	$\underline{\text{Disadvantages}}$ – administration is complicated, and it is not suitable for personal lines and unlimited covers.
Excess of Loss Reinsurance	 The reinsurer indemnifies the cedant for the amount above a certain excess/attachment point and up to an upper limit/detachment point. The insurer and reinsurer would have different claims experiences. There are three types of XOLs: Risk XL Aggregate XL Catastrophe XL Advantages – allows accepting large risks, reduces the risk of insolvency, stabilizes
	technical results, and makes efficient use of capital.
	$\underline{\text{Disadvantages}}$ – harder to price, and more complex than proportional covers
Stop Loss Reinsurance	An aggregate excess of loss reinsurance that provides protection based on the total claims, from all perils, arising in a class or classes over a period. The excess point and the upper limit are often expressed as a percentage of the cedant's premium income rather than in monetary terms.
Financial Reinsurance	A form of reinsurance involving less underwriting risk transfer and more investment risk/timing risk transfer from the cedant than in traditional reinsurance
Time & Distance Deals	A financial reinsurance arrangement whereby an insurer pays a single premium in return for a fixed schedule of future payments that match to the estimated liabilities of the insurer's claim outgo
Spread Loss Covers	Spread loss covers are arrangements where the insurer pays either annual or single premiums to the reinsurer to cover certain claims. These premiums, along with an agreed-upon interest, are accumulated in an experience account, which is settled at the conclusion of the multi-year agreement.
Financial Quota Shares	Financial quota share refers to an arrangement where commissions are provided primarily for financing purposes rather than for transferring risk.
Structured Finance	Reinsurers became involved in structured finance through their finite reinsurance business and the increasing need of financial guarantee insurers and investment banks for additional capacity.
Industry Loss Warranties	Provide reinsurance based on total industry losses from an event, rather than indi- vidual losses, with recovery triggered by the predefined industry loss threshold.
Run-off Reinsurance	Under such an arrangement, the 'book' is sold to the reinsurer who assumes all remaining premiums and all of the risk.
	Adverse Development Cover – A reinsurance arrangement whereby a reinsurer agrees, in return for a premium, to cover the ultimate settled amount of a specified block of business above a certain pre-agreed amount.
	<u>Loss Portfolio Transfer</u> – An arrangement where liabilities in respect of a specific book of business of an insurer is passed from one insurance entity to another.
Capital Market Products	 Insurers sometimes transfer risk directly to capital markets rather than reinsurers. Few capital market products are: Contingent Capital Insurance-linked securities

• Credit Securitization

E	EXTERNAL ENVIRONMENT	
Providers of Insurance	The major providers of insurance and reinsurance services are direct companies , reinsurers and self-insuring groups.	
Distribution of Direct Business	 Insurance business may be obtained through: Intermediaries like brokers, agents and banks Staff employed by direct insurers Direct marketing channels like the internet and telesales. 	
Self-Insuring Groups	Self-insuring groups include captives, pools, and P&I Clubs.	
Captives	 An entity set up with the primary purpose of insuring the risks of its parent company or associated group companies. Reasons for setting up a captive: Provide cover not available in the traditional insurance market Control overall insurance expenses of large companies Enables the corporate to buy cover for risk from reinsurers Ensures effective risk management Gain tax, legislative and regulatory advantages 	
Pools	An arrangement where parties collectively share premiums and losses for certain types of specific insurance coverages.	
Protection & Indemnity Clubs (P& I)	An association of ship owners to mutually cover certain types of marine risks.	
The London Market	The international face-to-face insurance and reinsurance market based in the City of London. Participants in the London Market include Lloyd's syndicates, sub- sidiaries of overseas (re)insurers, small reinsurance companies, self-insuring groups, and companies owned by a group of insurance and reinsurance companies.	
Lloyd's of London	Began in Edward Lloyd's coffee shop. Key participants include Names, Syndicates, Managing agents, Members agents, ILVs, and Lloyd's brokers.	
Names (Lloyd's)	Members of Lloyd's who provide capital to underwrite risks. Names may be indi- viduals or corporates.	
Syndicates (Lloyd's)	A group of Lloyd's Names who co-insure risks	
Integrated Lloyd's Vehicle (ILV)	Syndicates where the full participation is owned by insurance group companies	
Lloyd's Deposit	A deposit made by Lloyd's members with the Committee of Lloyd's before they underwrite any risk	
Lloyd's Managing Agent	An entity responsible for managing a Lloyd's syndicate. They would provide un- derwriting, technical, and administrative services.	
Lloyd's Member Agent	An entity that represents the interests of a Lloyd's Names. They take the resp sibility to introduce Names to various syndicates.	
Subscription system of Lloyd's	Business in the London Market is written through a subscription or slip system. The slip system is a mechanism used in the Lloyd's market where brokers prepar "slip" that outlines the details of an insurance or reinsurance risk. This slip is the presented to underwriters in the Lloyd's market, who review the risk and indic the proportion of the risk they are willing to accept.	
Funded Accounting	A method of accounting where all claims, premiums and expenses are allocated to the underwriting year in which the policy incepts.	

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One-Year Accounting	A method of accounting where all claims, premiums and expenses are alloc the accounting period, irrespective of when the policy incepts	cated to
Three-Year Accounting	A method of funded accounting where underwriting profits are only recogniz the end of the third accounting year from the start of the underwriting yea	
Reinsurance to Close (RITC)	An agreement for the transfer of all outstanding liabilities of an underwriti to a reinsuring party	ing year
Professional Standards	Actuaries should keep in mind all relevant professional and technical actuaries dards while determining a rate for an insurance coverage. These are issued IFoA and updated from time to time.	
Underwriting Cycle	A cycle of high and low insurance prices over a period of few years	
Soft Rates	The stage of an underwriting cycle when premiums and, hence, profitable high for the insurers in the market	ility are
Hard Rates	The stage of an underwriting cycle when premiums and, hence, profitability for the insurers in the market	are low
Regulations in General Insurance Reasons for Underwriting	 Regulations in General Insurance include: 1. Conducting external audits 2. Restrictions on the type of business 3. Limits on premium rates to be charged 4. Restrictions on using certain types of information 5. Requirements to deposit assets to back claims 6. Demonstration of solvency on a regular basis 7. Prescribed methods to find premiums or reserves 8. Restrictions on key role holders 9. Licensing for agents selling insurance 10. Payment of levies to consumer protection bodies 11. Protection of policyholders in case the insurer fails to honour prom 	ises
Cycle	 Low barriers to entry Delay until the profitability of the insurance business is known Simplistic capital requirements Economies of scale 	
Economic Factors affecting Business Environment	Economic factors include those that affect the insurance business due to cha the economy. Inflation, GDP growth, recession, expense inflation, etc. af insurance market.	-
Claims Inflation	Claims inflation could be of the following types:	
	 Price inflation Wage inflation Medical expense inflation Social inflation Courts awards inflation 	
Investment Income	Insurers invest premiums to earn income, with long-tailed lines benefitin. Pricing includes investment loadings, considering asset-liability duration, lissolvency, and economic conditions like interest and inflation rates.	-
Currency Fluctuation	Currency rate fluctuations affect insurers who write business in more the currency or in a currency different from their home/domestic currency. C rate fluctuations might distort underwriting results.	
Legal Factors	Legal factors include compensation awarded by the court to the claimants. would be made due to negligence or breach of contract.	Claims

ACTEX Learning	SP8 Summary Sheet 10	
Court Awards	Court awards compensation depends on the principle of indemnity. For property damage, compensation would be based on the cost of the lost materials/things/property accounting for depreciation. For bodily injury, compensation depends on the loss of income, medical costs, and compensation for pain and suffering.	
Legislative Factors	Changes in legislation would affect insurers and reinsurers. However, legislation takes time to draft and implement, giving insurers some time before the legislation comes in effect. Legislation might make certain insurance coverages compulsory. It may also have an impact on litigation.	
Social Factors –	Attitudes of society that may impact the insurance business are:	
Attitudes of Society	 Drink and driving Crime rates Attitudes of people towards insurance Organizations encouraging the placing of claims Staged accidents 	
Environmental Factors – Weather	Weather factors have an impact on the frequency and severity of claims. These factors include:	
	 Seasonality Subsidence and Land Heave Geography Global Warming Climate Change 	
Catastrophes	A catastrophe is a single event that can give rise to large aggregation of claims. Catastrophes can be natural or man-made.	
Latent Claims	Latent claims originate from perils that were not known when the policy was written. It could also mean claims that come into notice only after some years of the cause of loss. Examples of these are asbestos, Agent Orange, benzene, radiation from mobile phones, guns, nanotechnology, etc.	
Technological Factors	Changes in the technological space have helped insurers and reinsurers in all areas of their functioning, which lead to increasing efficiencies in insurance operations.	

RISK & UNCERTAINTY

Types of Uncertainty	Important types of uncertainties faced by general insurance companies are:• Process Uncertainty• Model Uncertainty• Parameter Uncertainty• Adjustment Factor Uncertainty• Data Uncertainty• Market Conditions Uncertainty
Process Uncertainty	The risk inherent in writing business, settling claims, and other general operations in general insurance. Process uncertainty can have an effect on the cost of claims as well as the other functions of an insurance company. Process uncertainty stems from external as well as internal sources.
External Sources of Process Uncertainty	 The external sources of process uncertainty include: Inherent Uncertainty of individual claims Changes in development pattern Demand surge Climate Change Third Party Behavior Legislative Changes

• Economic Conditions

ACTEX Learning	SP8 Summary Sheet	11
Internal Sources of Process Uncertainty	 The internal sources of process uncertainty include: Changes in business mix New Markets New Distribution Channels Changes in claims handling process Profit Sharing Arrangements 	
Effect of Process Uncertainty on other functions of business	Process Uncertainty would impact not just claims but other areas of well. Few examples are as follows:• Aggregators• Competition• Off-shoring• Insurance Cycle• Investments• Expense Uncertainty	business as
Parameter Uncertainty	The risk that an inappropriate parameter has been used in the model. uncertainty stems from: • Uncertainty from data used • Uncertainty from format of data • Exceptional claims • New distribution chann	ilosophy
Model Uncertainty	 The risk of using a model that is not appropriate for the purpose. Model stems from Model error Programming error Incorrect distributional assumptions 	incertainty
Sources of Data	DATA OSED IN TRICING The data used for pricing can come from two main sources: Internal Sources own historical data of premiums and claims External Sources data from industry wide sources	
Industry-wide Data Collection Schemes	Industry-wide collection schemes collect data from their member office make summaries of this data available to all their members.	s and then

Merits: Advantages of industry-wide data collection schemes are:

- 1. Helps compare insurer's experience with that of the industry
- 2. Helps to understand competitors' businesses
- 3. Benchmark development factors may be obtained for reserving

Demerits: Disadvantages of industry-wide data collection schemes:

- 1. Potential for distortion owing to heterogeneity
- 2. Data less flexible than internal data
- 3. Data might be out of date
- 4. Not all companies contribute to the scheme
- 5. Quality of data depends on quality of data supplied by members
- 6. Data provided by companies may not be comparable because of differences in geographies, policies sold, practices, data stored.

The availability of quantity and quality of data varies:

• within organizations

Factors affecting Quality and

Quantity of Data

- between organizations
- between different classes of business

SP8 Summary Sheet

Variation within Organization	• •	n organization due to different distribution channels h brokers, agents, or directly with customers. This y of data.
Variation between	The following factors affect the	e quality of data between organizations:
Organizations	Size and age of the compLegacy systemsIntegrity of systems	Management & StaffNature of the organization
Variation by Line of Business	\tilde{c}	e quality of data between lines of business:
Uses and Users of Data	The uses and users of data ma	y be summarized as follows:
	Uses (Functions)	Users (Professionals involved)
	Administration	Management, Claims Adjusters
	Accounting	Accountants
	Statutory Returns	Actuary, Management
	Investments	Investment Professionals
	Management Information	Senior Management
	Risk Management	Risk Team, Actuaries, Reinsurance
	Pricing	Underwriters, Actuaries
	Reserving	Claims Adjusters, Actuary
	Capital Modelling	Actuaries
	Marketing	Marketing Staff
	Experience Statistics	Actuaries, CAT team
Information Systems	An insurer/reinsurer would be order to gather, input, store ar	e required to develop robust information systems in ad manage data effectively.
Proposal Form	information source. Common insured, estimated sum insured	formation regarding the policyholder and is a prime items on the proposal form include details of the , risk factors based on the class of business, excess on this form should also be unambiguous, well-designed
Claims Form	The claim form will be the main source of information for claim related detail regarding a policy.	
Features of Premium	Important features of premium	a that should be recorded are:
Information	Written and signed amoPayment datesPremium adjustments	untsCommissions & DiscountsCross-selling
Features of Claim Information	Important features of claim inf	formation that must be recorded are:
	 Definition of claims Estimated outstanding a Multiple claim payments Reopened claims 	

Policy Data required	For direct insurance & facultative rei	insurance , we need the following data:
for Pricing	 Dates on cover Policy limits Excess Company's share of total risk Rating factors 	 Details of premium charged Type of coverage Exclusions Policy number linked to claims information
	For treaty reinsurance , we would also r	need the following information:
	 Type of reinsurance Basis of cover Treaty limits Aggregate limits and Excess points 	 5. Reinstatement premiums 6. Treaty terms 7. Reinsurer's share of loss or limit
Claims Data required	Claims data required for pricing includes:	
for Pricing	 Date of claim event Status of claim Date closed Date reported Date, amount of claims payments Payment type Outstanding claim payments 	 Currency of claim payments Rating factor details Type of claim Type of peril Policy number to link with policy information Unique claim identifier
Sources of Data Error	Few potential sources of data error are:	
	Wrong claim numberWrong policy numberWrong risk details	Wrong claim dateWrong payment datesWrong claim type
Sources of Data Distortion	Few potential sources of data distortion a	re:
	 Changes in claim handling procedure Case estimates Processing delays 	Large claimsReturn premiumsClaims inflation
Prevention of Errors	Few measures to ensure prevention of error	ors are:
	 Data inputs should be checked and Ensure consistency in practices ove Digits entered should be checked Minimum and maximum values to Train staff and employees before the 	r time to minimize errors be checked
Effect of Inadequate Data	The impact of inadequate data on pricing	include:
on Pricing	 Wrong premium rate being charged Errors in apparent risk in force Errors in apparent claims experiend True distributions of business betw Underwriting losses if rates are too Decrease in market share if rates an Adverse selection risks 	ce een different risk groups distort low
Pricing with Limited Data	When data is limited, the following method	ods could be used:
	 Use of other data Margins Use of ILFs Qualitative data 	

AC	TUARIAL INVESTIGATIONS
Premium Rate Analyses	 In order to analyse the premium rates, we follow the steps as below: Project ultimate claim costs using projection techniques Compare actual vs expected claims, adjusting for abnormalities Project future experience. Factor in uncertainties and future trend assumptions Evaluate the rating structure. Use one-way, two-way, or multivariate rating models Compare final rates with external market data Modify rates based on long-term customer value Reassess past profitability using updated premium rates
Expense Analysis	 Expense analysis is important for the following reasons: Helps allocate expenses correctly between different groups Provides useful insights into the insurer's financial plans Provides information to management Provides information to be shown in statutory returns We divide expenses into Direct v/s Indirect Expenses and Fixed v/s Variable Expenses. After this, expenses must be split into homogeneous cells.
Direct Expenses	Expenses that can be allocated to specific policies, whether new business acquisition or administration of business already written.
Indirect Expenses	Expenses that relate to general management and service departments
Fixed Expenses	Expenses that do not vary with the amount or volume of business written
Variable Expenses	Expenses that vary with the volume of business written
Types of expenses Treatment of Certain Expenses	 Expenses other than commission can be split into: Initial Expenses Administration Expenses Renewal Expenses Claims Expenses Investment Expenses It is difficult to split certain expenses into required cells because it is not easy to
	identify which cell they belong to. Hence, approximate methods are used to get the split. Examples of how a few expenses could be split are given below:
	Salaries – Salaries are fixed in the short run but variable long-term, allocated directly for single-cell employees, split via timesheets for multi-cell employees, and classified as direct or indirect for admin staff.
	Property Costs – Charge actual/notional rent, allocate based on floor space and salary proportions.
	Computer Costs – Distribute expenses based on departmental computer usage.
	${\bf Investment} \ {\bf Costs} - {\rm Deduct} \ investment \ expenses \ from \ expected \ return$
	<u>Capital Costs</u> – Amortize one-off costs over the product life.
	$\underline{\text{Claims Handling Costs}}_{\text{costs by claim volume.}} - \text{Allocate direct costs to specific cells; distribute indirect costs by claim volume.}$

Reasons for Monitoring Business	 The main reasons for monitoring business are: Assessing performance Risk management Market intelligence Regulatory requirements Influencing the market Reserving Actuarial Control Cycle
Factors to be Monitored	 An insurer needs to monitor the following factors: 1. Premium rate changes 2. Portfolio Movements 3. Volumes of Quotation 4. Persistency & Profitability by Source
Portfolio Movements	 Portfolio movements refer to changes in the underlying risks of the business written. It is important to monitor movements to manage the volume and mix of business, manage cross subsidy, and manage the growth of business. Portfolio movements can be in terms of: Lapses or renewals New volumes Strike Rates Cancellations Endorsements Mix of business
Premium Rate Changes	Premium rate change could be defined as: $\mathbf{Rate Change}_{t_1 \to t_2} = \frac{\mathbf{Premium Rate}_{t_2}}{\mathbf{Premium Rate}_{t_1}} - 1$ Methods to calculate premium rate changes are: • Direct calculation • Price of a standard risk • Underwriter's view of rate change • Rate change at renewal - the formula for this: $\mathbf{Rate Change}_{t_1 \to t_2} = \frac{\sum \mathbf{Premium}_{t_2}}{\sum \mathbf{As} - \mathbf{if Premium}_{t_1}} - 1$ where $\mathbf{As} - \mathbf{if Premium}_{t_1} = \mathbf{Premium}_{t_1} \times \frac{\mathbf{ILF} @ \mathbf{Lim}_{t_2} - \mathbf{ILF} @ \mathbf{Attach}_{t_2}}{\mathbf{ILF} @ \mathbf{Lim}_{t_1} - \mathbf{ILF} @ \mathbf{Attach}_{t_1}} \times \frac{\mathbf{Share}_{t_2}}{\mathbf{Share}_{t_1}} \times \frac{\mathbf{Exp}_{t_2}}{\mathbf{Exp}_{t_1}}$
Lapses/Renewals	Lapse rate is the ratio of the number of policies lapsed to the total number of policies invited for renewal. Renewal rate is the complement of this.
New Volumes	New business rate can be measured in a similar way as the lapse rate. Instead of using an exposure measure in the denominator, we use the same number of policies invited for renewals.
Strike Rates	The ratio of the number of written policies to the number of quoted policies in a given period. Also called conversion rate.
Cancellation Rate	The ratio of cancelled policies to the number of policies invited for renewal in a particular period.

Collective Risk Models

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This would help to assess the success of marketing campaigns.Persistency and Profitability by SourceInsurers would measure profitability by branch, broker, and direct business. Th helps to understand which source provides better quality and long-lasting businesUse of Actuarial InvestigationsThe results of actuarial investigations are used for: 1. Carrying out profit testing exercises 2. Estimating price elasticity curves 3. Creating lifetime pricing models 4. Redesigning rating tariffs 5. Deciding reinsurance needs 6. Feeding into other processes like capital modellingFeatures of systems to monitor BusinessDesirable features of a system for monitoring business include: 1. Output must be concise and tailored 2. Data must be reliable and validated 3. Calculations must be valid 4. Results must be valid 4. Results must be complex 7. Systems must be documented and low maintenance 8. Results must be clear and easy to interpret 9. Output must be consistent with other data sources 11. Outputs must be consistent with other analyses	Endorsements	Endorsements are changes made to a policy due to changes in the underlying riskThe endorsement rate is defined as the ratio of the number of endorsements duringa period to the number of policies exposed for the same period.
This would help to assess the success of marketing campaigns.Persistency and Profitability by SourceInsurers would measure profitability by branch, broker, and direct business. The helps to understand which source provides better quality and long-lasting businessUse of Actuarial InvestigationsThe results of actuarial investigations are used for: 1. Carrying out profit testing exercises 2. Estimating price elasticity curves 3. Creating lifetime pricing models 4. Redesigning rating tariffs 5. Deciding reinsurance needs 6. Feeding into other processes like capital modellingFeatures of systems to monitor BusinessDesirable features of a system for monitoring business include: 1. Output must be concise and tailored 2. Data must be reliable and validated 3. Calculations must be valid 4. Results must be valid 4. Results must be complex 7. Systems must be documented and low maintenance 8. Results must be clear and easy to interpret 9. Output must be consistent with other data sources 1. Outputs must be consistent with other analyses	Mix of Business	Change in the mix of business may result in change in profitability levels.
by Sourcehelps to understand which source provides better quality and long-lasting businesUse of ActuarialThe results of actuarial investigations are used for:Investigations1. Carrying out profit testing exercises2. Estimating price elasticity curves3. Creating lifetime pricing models4. Redesigning rating tariffs5. Deciding reinsurance needs6. Feeding into other processes like capital modellingFeatures of systems tomonitor Business1. Output must be concise and tailored2. Data must be reliable and validated3. Caclulations must be valid4. Results must be validated5. Data must be easy to collect6. Calculations must be documented and low maintenance8. Results must be clear and easy to interpret9. Output must be consistent with other data sources11. Outputs must be consistent with other analyses	Volume of Quotation	An insurer would track the changes in the number of quoted policies over time. This would help to assess the success of marketing campaigns.
Investigations1. Carrying out profit testing exercises2. Estimating price elasticity curves3. Creating lifetime pricing models4. Redesigning rating tariffs5. Deciding reinsurance needs6. Feeding into other processes like capital modellingTestawers of systems tomonitor Business1. Output must be concise and tailored2. Data must be reliable and validated3. Calculations must be valid4. Results must be validated5. Data must be easy to collect6. Calculations must be documented and low maintenance8. Results must be documented and low maintenance8. Results must be consistent with other data sources11. Outputs must be consistent with other analyses		Insurers would measure profitability by branch, broker, and direct business. This helps to understand which source provides better quality and long-lasting business
monitor Business1. Output must be concise and tailored2. Data must be reliable and validated3. Calculations must be valid4. Results must be validated5. Data must be easy to collect6. Calculations must not be complex7. Systems must be documented and low maintenance8. Results must be clear and easy to interpret9. Output must be consistent over time10. Inputs must be consistent with other data sources11. Outputs must be consistent with other analyses		 Carrying out profit testing exercises Estimating price elasticity curves Creating lifetime pricing models Redesigning rating tariffs Deciding reinsurance needs
production of results.	-	 Output must be concise and tailored Data must be reliable and validated Calculations must be valid Results must be validated Data must be easy to collect Calculations must not be complex Systems must be documented and low maintenance Results must be clear and easy to interpret Output must be consistent over time Inputs must be consistent with other data sources Outputs must be consistent with other analyses There must be minimum delay between data the cut-off date and the

Individual Risk Models Individual Risk Model considers a fixed number of risks in a portfolio. Assumptions of this model are:

- 1. Risks are independent
- 2. Claim amounts are not necessarily identically distributed
- 3. Number of risks do not change over time
- 4. There can be no more than one claim for each risk

Assumptions of this model are:

- 1. Claim amounts X_i are independent and identically distributed
- 2. Claim amounts X_i and random variable for claim number N are independent of each other

Total claim amount, S, payable during a specified period is given by:

$$S = X_1 + X_2 + X_3 + \dots + X_N$$

where X_i is claim amount in respect of the *i*-th claim and N (a random variable) is the number of claims during the period.

Mean of S:

$$E(S) = E(X)E(N)$$

Variance of S:

$$\operatorname{Var}(S) = E(N)\operatorname{Var}(X) + [E(X)]^2\operatorname{Var}(N)$$

 $\underline{\mathbf{MGF} \ \mathbf{of} \ S}:$

$$M_S(t) = M_N[\log M_X(t)]$$

Recursive formula for G(x)

The recursive formula for the probability of r number of claims, i.e., P[N = r] is given by:

$$P[N=r] = p_r = \left(a + \frac{b}{r}\right)p_{r-1}$$
 for $r = 1, 2, 3, \dots$

The recursive formula for the probability of r aggregate claim amount, i.e., P[S = r] is given by:

$$P[S=r] = g_r = \sum_{j=1}^r \left(a + \frac{bj}{r}\right) f_j g_{r-j} \text{ for } r = 1, 2, 3, \dots$$

where:

- a & b are constants that depend on the claim frequency distribution N; and
- $f_j = P[X_i = j]$
- $g_0 = p_0$

Normal Approximation to G(x) When E(N) is large, we may assume that S follows a Normal Distribution with mean μ and variance σ^2 . Therefore,

$$G(x) = P[X \le x] = P\left[\frac{S-\mu}{\sigma} \le \frac{x-\mu}{\sigma}\right] \approx \Phi\left(\frac{x-\mu}{\sigma}\right)$$

We may estimate μ and σ as:

$$\mu = E[S] = E[N]E[X],$$

$$\sigma^{2} = E[N]\operatorname{Var}[X] + [E(X)]^{2}\operatorname{Var}[N].$$

Translated Gamma Approximation to G(x)

We equate means, variances and coefficient of skewness of S and k + Y, we get:

$$\mu = k + \frac{\alpha}{\delta},$$
$$\sigma^2 = \frac{\alpha}{\delta^2},$$
$$\beta = \frac{2}{\sqrt{\alpha}}.$$

From the above three equations, we estimate k, α and δ from the known values of μ, σ^2 , and β , which are mean, variance and coefficient of skewness of S, respectively.

Stochastic simulations may be used to approximate a distribution for aggregate claims, i.e., G(x). This requires to simulate number of claims.

Stochastic Simulation

RATING METHODOLOGIES

Categories of Pricing	The General Insurance Premium Rating Issues Working Party (GRIP) has outlined five categories of pricing:
	 Tariff - Regulators influencing premium rates Qualitative - Rates based on subjective factors Cost plus - Rates based on statistical methods Distribution - Rates based on non-cost elements Industrial - Rates based on operational efficiency
Components of Pricing	The "technical premium" has the following components:
	Risk Premium – consists of pure risk rate and loading for CAT and large loss
	Office Premium – cost of reinsurance, expenses, cost of capital, investment income
	Other Considerations – rating factors, practical considerations
Pure Risk Premium	 Pure risk premium may be estimated using the following steps: 1. collection of relevant data 2. adjusting and grouping of data 3. selection of appropriate rating model 4. analysing the data 5. setting assumptions required by the model 6. testing the assumptions for goodness of fit 7. running the model to arrive at an estimate of cost of claim 8. performing sensitivity and scenario testing
Homogeneity of Data	 Data needs to be grouped into homogeneous cells where risks in each cell represent similar characteristic. Reasons for grouping data include: avoiding unintentional cross-subsidies ensuring profitability will not depend on the cross section of risks gaining market acceptance when launching a particular risk division
Trending Data	Past data is subject to change over time due to various reasons. Past data needs to be trended for:• Unusual base experience• Changes in underwriting• Trends in claim experience• Changes in perils covered• Inflation• Changes in self-retention limits• Changes in mix of risks• Changes in legislative factors• Changes in distribution methods• Advancements in technology• Changes in coverage• Medical advances• Changes in claim settlement procedures• Changes in construction of property
Projecting Claims & Exposure	To arrive at the risk premium, we divide projected claims by projected exposure values. <u>Projecting Claims</u> – For projecting claims, we first project claims with adjustments and trends. Then claims need to be projected to ultimate. <u>Projecting Exposure</u> – When exposure units are measured in monetary terms, base exposure values should be projected using an appropriate inflation rate, which may differ from the rate applied to claim costs. This projection should only extend to the midpoint of the exposure period for the new rates.

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Catastrophe and Large Claims Loading	 When analysing claims, we separate attritional claims from large and catastrophe claims. For catastrophe losses, we estimate their cost from a proprietary catastrophe model. For non-catastrophe large losses, the cost can be estimated based on: omitting them from the analysis and allowing separately in the risk premium truncating large losses to a certain point and spreading any cost above this level across a large portfolio of risks leaving large losses in the claims data and conducting the analysis
Office Premium	The office premium is the risk premium adjusted for the cost of reinsurance, expenses, profit loading, and investment income.
Cost of Reinsurance	Reinsurance premium can be incorporated in two ways:1. as the net cost of reinsurance based on the gross risk premium2. as the gross cost of reinsurance based on the net risk premium
Expense Loading	Commissions, expenses and other margins may be incorporated by either adding an overall percentage or splitting fixed and variable expenses.
Profit Loading	In order to give a reasonable return to shareholders or capital providers, a profit loading would also be added to the premium rates.
Investment Income	Investment income is expected to be earned on the premium received by the insurer. This would also be allowed for in the premium rate. This can be done by discounting the cost of claims and expenses at a suitable rate of interest to the date when the premium is paid.
Other Considerations in Rating	After arriving at the office premium, we consider the rating factors and practical considerations.
Rating Factors	The rigor of underwriting depends on class of business. For personal lines , underwriting is completely based on the rating factors. For commercial lines , like commercial fire, underwriting is a skill-based job based on reports.
Conditions of Good Rating Factors	 A good rating factor should satisfy the following conditions: defines the risk clearly does not correlate too closely with other factors is practical to obtain and record is objective is factual and verifiable is acceptable to the policyholder is based on current factors used in the market
Selection of Rating Factors	To select rating factors, we perform an ANOVA exercise. This includes:
	One-way analysis – the amount of variability explained by each factor
	$\underline{\text{Two-way analysis}}$ – each factor is investigated along with its correlation with others
	$\underline{\mbox{Multivariate analysis}}_{\mbox{for all factors and correlations}}.$
Practical Considerations	The actual premium charged may be different from the theoretical office premium due to the following factors: Business Objectives Competitive Pressures Difficulty in establishing price Insurance cycle Section 2017 Secti

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Other Influences on Pricing

Other influences include:

- Competition and the need to maintain or build market share
- Availability of capital to support new business
- Impact of reinsurance capacity
- Sophistication of sales and quotes system
- Demands of regulators
- Relationships with brokers and distributors
- Differences between "direct" approach and traditional routes

FREQUENCY-SEVERITY & BURNING COST RATING

From the Ground Up (FGU)	A statement that details insurer's claim experience is said to be "from the ground up" when it includes the number and distribution of all claims, irrespective of the size.	
Aggregate Deductible	The maximum amount that the insurer is responsible for paying when all losses are combined.	
Non-Ranking Deductible	The portion of deductible applied to each individual loss that does not contribute to the insurer's aggregate deductible.	
Ranking Deductible	The portion of deductible applied to each individual loss that contributes to the th insurer's aggregate deductible.	
Trailing Deductible	The amount that the insured retains for each individual loss after the aggregate deductible has been completely exhausted.	
Per Occurrence Limit	The maximum amount that the insurer would retain for each loss	
Annual Aggregate Limit	The maximum amount the insurer will cover for all losses arising during a one-year policy period.	
Frequency-Severity Approach	This method estimates claim frequency and severities separately and then combines them to estimate the expected cost of claims. <u>Advantages</u> – mirrors the underlying process, complex structures may be priced, helps identify trends, additional insights into loss amounts. Disadvantages – data requirements are onerous, time-consuming process, requires	
	high level of expertise.	
Data Requirements for F-S Approach	There could be issues with the data in terms of form, consistency, and choice of base period. In addition to the data requirements discussed in Chapter 6, the following data would be needed:	
	 Submission Documents Exposure Information Individual Claim Information 	
Trending for F-S Approach	Trends need to be applied separately for frequency and severity under the F-S method. While trending, we must:	
	• Project historical frequency and severity in line with trends assumed to current values; and	

• Project them to the mid-point of the future exposure period

Frequency Trends	Causes of frequency trends include changes in: • Accident frequency
	Accident frequencyPropensity to make claims due to social inflation
	Legislation
	• Structure of risk
	Frequency is calculated as:
	$Frequency = rac{Ultimate number of losses}{Exposure measure}$
	Exposure measure
Severity Trends	Causes of severity trends include:
	• Economic inflation
	• Economic conditions
	• Changes in court awards
	• Changes to the structure of risk
	Severity is calculated as:
	$\mathbf{Severity} = rac{\mathbf{Ultimate\ cost\ of\ loss}}{\mathbf{Ultimate\ number\ of\ losses}}$
Developing Losses in F-S Approach	After adjusting individual losses for trends, it is important to project them to their ultimate levels since past claims may not be fully developed. Methods that may be used to develop losses include:
	1. Applying an incurred development factor to each individual loss
	2. Developing only open claims using "case estimate" claims ratio
	3. Estimating IBNR based on known losses from a cohort of claims
	4. Using stochastic development methods to consider variation in individual ultimate loss amounts
Fitting Distributions in F-S Approach	After adjusting the historical data for trends and developing individual losses, we fit frequency and severity distributions. The stages involved in fitting the distributions are:
	Stage I: Choice of base period – Older policy years give reliable but less relevant estimates, so we may exclude recent years, exclude underdeveloped years, or weight developed years more.
	Stage II: Choice of distribution – Common distributions used for claim severity are Log-Normal, Weibull, Pareto, Gamma, and Generalized Pareto. Distributions used for claim frequency are Poisson and Negative Binomial.
	Stage III: Parameter estimation – Parameters may be estimated using the method of moments, least-square estimates, or maximum likelihood estimates
	Stage IV: Testing Fit – The fit must be checked using statistical methods.
K-S GoF and A-D GoF tests	Kolmogorov-Smirnov GoF – This test checks if a given sample comes from a speci- fied distribution by comparing the empirical distribution of the sample to the expected cumulative distribution.
	<u>Anderson-Darling GoF</u> – This test is similar to the K-S GoF, where the test statis- tics measures the difference between the empirical distribution of the sample and the CDF of the assumed distribution. However, the A-D GoF test places more weight on the differences in the tails of the distribution. The A-D GoF test is more sensitive to deviations in the tails and more powerful than the

K-S GoF.

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Burning Cost Approach	Burning cost is the cost of claims expressed as an annual rate per unit of exposure.
	$\underline{\text{Advantages}}$ – simple, less data onerous, quicker, experience of individual risk or portfolio of risk can be allowed for
	$\underline{\mbox{Disadvantages}}$ – difficult to spot trends, making adjustments is difficult, a crude approach.
Data Requirements for Burning Cost Approach	In addition to the data requirements discussed in Chapter 6, policy data and esti- mated outstanding claim amounts need to be known.
Burning Cost Premium	The premium is given by:
	Burning Cost Premium = $\frac{\sum \text{Claims}}{\text{Total Exposure}}$
Trending in Burning Cost Approach	Exposure and claim amounts need to be projected to current levels. Different approaches may be used to trend past data.
Developing Losses in Burning Cost Approach	Without individual loss data, assumptions will be less detailed than in the frequency-severity method. IBNR factors are typically derived from individual risk data or aggregated business results, with adjustments for inflation and insights from

RATING USING ORIGINAL LOSS CURVES

recent reserving exercises if relevant.

Introduction	Original Loss Curves are used in general insurance to price layers at which data is too sparse to derive a premium rate.	
Types of Curves	The most used forms of original loss curves are: $\underline{\text{Exposure Curves}}_{\text{cated to different primary coverage limits, or deductibles.}}$	
	$\underline{\text{Excess of Loss Scales}}_{\text{tion of premium to be allocated to excess layers rather than primary layers.}$	
	<u>Increased Limit Factors</u> – They are a table of multiplicative factors giving the ratio of premium for higher limits to basic limit premium.	
Properties of Original Loss Curves	If: • X is a random variable representing severity • $F_X(x)$ is the CDF of X • $S_X(x) = 1 - F_X(x)$ • $LEV_X(x)$ is the Limited Expected Value distribution of X We have, $LEV'_X(x) = S_X(x)$	
	 Hence, the properties of loss curves are: <i>LEV(x)</i> is an increasing function 	

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Property Business -Use of Exposure Curves They are defined as:

$$G(x) = \frac{LEV_Y(x)}{E[Y]}$$

where Y is a random variable that represents the size of loss (X) as a proportion to the measure of risk (M). Hence, $Y = \frac{X}{M}$. G(x) is a curve that represents the ratio of total claims cost up to a specific point x to the overall claims cost, where x is the selected proportion of maximum claim. Steepness of G(x) would depend on the severity of the underlying loss distribution. Exposure curves may be used to price a property XL treaty having a structure L excess of D, using the following formula:

$$C_L = C \times \left(G\left(\frac{L+D}{M}\right) - G\left(\frac{D}{M}\right) \right)$$

where

- C_L is the claim cost to the layer priced
- C is the ground-up loss cost

The relative loss size distribution is given by the random variable $Y = \frac{X}{M}$. An important assumption underlying exposure curves is that Y is independent of the size of risk. However, this assumption holds true only when the data is homogeneous.

The steps involved in pricing a property excess of loss treaty include:

- 1. Gather original premium and sum insured data categorized in bands
- 2. Estimate a representative sum insured for each band
- 3. Estimate an original loss ratio
- 4. Adjust treaty limits for inflation and trends
- 5. Choose an appropriate **exposure curve** for the line of business
- 6. Express the attachment and detachment points of the layer as a proportion of sum insured $(Y_1 \text{ and } Y_2)$
- 7. Determine $G(Y_1)$ and $G(Y_2)$ from the selected exposure curve
- 8. Compute the loss cost to layer using $G(Y_2) G(Y_1)$
- 9. Derive the **loss rate** as the total loss cost to the layer divided by the total premiums

The following considerations need to be accounted for:

- Homogeneity of Data
- Claims Inflation
- Choice of Exposure Curve
- Estimation of Original Loss Curve
- Original Deductibles
- Inuring Reinsurance
- Stacked Limits

The steps in deriving exposure curves include:

- 1. Collect claims data regarding the amount paid, risk size, and cause of loss
- 2. Express each claim as a percentage of the risk size
- 3. Group the data into homogeneous groups based on perils
- 4. Construct a table of losses as a percentage of risk (x%). We find the total value of losses less than or equal to x% of PML (Let this be B). Then, we calculate the first x% of losses greater than x% of PML (Let this be C).
- 5. Find the total accumulated loss costs as the sum of B and C.
- 6. Finally, the empirical exposure curve is found as the ratio of (B + C) to B.
- 7. Combine groups for which there is no significant difference
- 8. Smoothen the empirical curves

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Steps in Property XL using Exposure Curves

Relative Loss Distribution

Considerations in Exposure Curves

Deriving Exposure Curves

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Casualty Business

Steps in Casualty

XL using ILFs

ILFs are used in casualty rating due to the lack of an upper limit on loss amounts.

$$ILF(x) = \frac{LEV_X(x)}{LEV_X(b)}$$

ILFs may be used to price a casualty XL treaty having a structure L excess of D, using the following formula:

$$C_{L} = C_{b} \times (ILF(L+D) - ILF(D))$$

where:

- C_L is the cost to the layer priced
- C_b is the basic limit loss cost

We may follow the same steps to price a casualty XL treaty as used with exposure curves when pricing a property XL, however, with the following differences:

• For casualty XL pricing, we estimate the loss cost for the original limit as a starting point. This is given by:

 $C_I =$ Original Limit Loss Cost $= C_b \times ILF(I)$

• The layer loss cost then changes to:

$$C_L = \text{Layer Loss Cost} = C_I \times \left(\frac{ILF(L+D) - ILF(D)}{ILF(I)}\right)$$

When using ILFs, the following considerations need to be made: 1. Treatment of expenses

- 2. Claims inflation
- 3. Treaties on cession basis

When deriving ILFs, a few problems may be faced, such as the lack of volume of data, unavailability of information on large loss, losses adjusted for trends, and claims might not be closed.

ILFs may be derived using the methodology devised by ISO in the US.

Empirical Survival Function The survival function is given by:

$$\hat{S(u_n)} = \prod_{i=1}^n \hat{CSP(i)} = \prod_{i=1}^n \frac{Nu_i}{NI_i}$$

Curves used in Practice

Some curves used in practice by reinsurers are:

- 1. Curve fitting
- 2. Riebesell curves
- 3. Market curves

Advantages & Disadvantages of Loss Curves

Advantages – Simple to implement, easy to explain, loss cost internally consistent, use with less data available

Disadvantages - Application may be difficult, sensitive to the curve chosen, market wide data collection

Considerations in using ILFs **Deriving ILFs**

GENERALIZED LINEAR MODELS

Multiple Linear Regression

A multiple linear regression model with k parameters representing the relationship between response variable Y_i and independent variables $X_i k$, takes the form:

$$Y_i = \beta_0 + \sum_{j=1}^k \beta_j f_j(X_{ij}) + \varepsilon_i$$

where

- β_j is the *j*-th parameter value
- ε_i are error terms

The parameters of the model can be estimated using the method of maximum likelihood estimates.

Exponential Family

The exponential family is a set of distributions whose PDF can be written in the form:

$$f(y; \theta, \varphi) = \exp\left(\frac{y\theta - b(\theta)}{a(\varphi)} + c(y, \varphi)\right)$$

where

- $a(\varphi), b(\theta)$ and $c(y, \varphi)$ are specific functions depending on the distribution.
- θ is the canonical and φ is the scale parameter.

The **mean and variance** of Y are given by:

$$\mu = E[Y] = b'(\theta) = \mu(\theta_i),$$

Var[Y] = $a(\varphi)b''(\theta).$

The **variance function** is defined as:

$$V[\mu] = b''(\theta)$$
 Pure premium data is challenging to model due to a spike at zero and a wide

range of positive values. The Tweedie distribution addresses this by allowing a variance function proportional to μ^p , accommodating both zero-inflation and claim

Tweedie Distribution

Generalised Linear Models

The multiple linear regression generalizes into the following GLM structure:

$$Y_i = g^{-1} \left(\sum_{j=1}^k X_{ij} \beta_j + \xi \right) + \varepsilon_i$$

where

variability.

- ε_i is the error term
- ξ is an offset or known effects

The important components of a GLM are:

 $\frac{\text{Distribution of response variable}}{\text{ily.}} - Y_i \text{ has a distribution from the exponential fam-}$

<u>Linear Predictor</u> – The linear predictor, η , is a function of co-variates given by:

$$\eta = \sum_{j=1}^{k} X_{ij}\beta_j + \xi$$

<u>Link Function</u> – Connects η with μ . The relationship is:

$$\mu = g^{-1}(\eta)$$

If other distributions are used, other methods are used.

If the distribution of response variables is the Normal Distribution and the link

function used is the identity link, the parameters may be estimated using the equa-

 $\beta = (X^T X)^{-1} X^T Y$

GLMs can be used in general insurance pricing to predict the claim frequency, claim

Response Variable – could be claim frequency, average claim amount or loss ratios

Independent Variables - could be the rating factors (Categorical and Numerical)

Interaction Term – An interaction term improves the model by capturing the combined effect of multiple factors, adding predictive value beyond individual

 $d(Y_i; \mu_i) = 2\omega_i \int_{i=1}^{Y_i} \frac{Y_i - \zeta}{V(\zeta)} d\zeta$

 $D = \sum_{i=1}^{n} d(Y_i; \mu_i)$

 $D^* = \frac{D}{\omega}$

Scaled deviance is the ratio of deviance to the scale parameter, defined as:

that affect cost of claims depending on the class of business.

Let d be each observation's contribution to the deviance defined by:

Estimating Parameters of a GLM

Applications of GLM in Insurance Pricing

Deviance

Important statistical tests are:

Analysis of Significance of **Factors - Statistical**

Analysis of Significance of

Factors - Graphical

Residuals

The total deviance is therefore defined as:

Chi-Squared Test – Two nested models may be compared using the test:

$$D_1^* - D_2^* \sim \chi^2_{df_1 - df_2}$$

F-Statistics – If the scale parameter is not available, this test will test:

$$\frac{D_1 - D_2}{(df_1 - df_2)\frac{D_2}{df_2}} \sim F_{df_1 - df_2, df_2}$$

Akaike Information Criteria – The lower the AIC, the better the model

Graphical methods used to analyze the significance of factors include:

- Hessian Matrix
- Comparison with expectations
- Comparison over time
- Consistency check with other factors

Residuals show how the fitted values differ from actual observations.

Deviance Residuals – The deviance residuals is defined as:

$$r_i^D = sign(Y_i - \mu_i)\sqrt{d(Y_i; \mu_i)}$$

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tion:

size, or loss ratios.

factors.

for a class of business.

Pearson Residuals The Pearson residual is defined as:

$$r_i^p = \frac{Y_i - \mu_i}{\sqrt{\frac{\varphi V(\mu_i)(1 - h_{ii})}{\omega_i}}} = \frac{Y_i - E[Y_i]}{SD[Y_i]\sqrt{1 - h_{ii}}}$$

where h_{ii} is called the leverage and is the *i*th diagonal element of the hat matrix:

$$H = X(X^T X)^{-1} X^T$$

The value of the Pearson residual ranges from 0 to 1. A value close to 1 means that the observation heavily influences the prediction, making the residual error small.

The residual patterns of models of average costs, frequency, etc. may be plotted. A good model should produce residuals that:

- are symmetrical about the x-axis
- have an average residual of zero
- are fairly constant across the width of fitted values

Cook's distance for the i-th data point is defined as:

$$c_i^p = \frac{h_{ii}}{(1 - h_{ii})(\sum h_{ii})} \times (r_i^p)^2$$

Interactions may be expressed in two ways:

<u>Complete Interactions</u> – This considers a single factor representing every combination of the two factors.

 $\frac{\text{Marginal Interactions} - \text{This considers single factor effects of the two factors and}{\text{the additional effect of an interaction term over and above the single factor effects.}$

Aliasing occurs due to linear dependency among the observed independent variables X_1, X_2, \ldots, X_P .

- Intrinsic Aliasing This occurs due to inherent dependencies in the definition of covariates. This is commonly observed when categorical covariates are used.
- Extrinsic Aliasing This occurs when covariates are dependent due to data characteristics rather than inherent properties. It happens when one factor is perfectly correlated with another.
- <u>Near Aliasing</u> This occurs when two or more factors contains levels that are almost, but not quite, perfectly correlated.

 Parameter Smoothing
 Parameter smoothing is the process of adjusting parameter estimates to reduce volatility, prevent overfitting, and ensure a more stable model. There are four methods to factor simplification:

- group and summarize data prior to loading
- grouping in the modelling package
- curve fitting
- piecewise curve fitting

Offsetting

Offsets are used to fix the relativities of a factor to a set of values that would differ from naturally fitted values. For example, to fit NCD in GLMs.

Residual Plots

Cook's Distance

Complete & Marginal Interactions

Aliasing

MULTIVARIATE MODELLING

Information on Proposal Form - Motor Insurance	A motor insurer would seek the followin	A motor insurer would seek the following information when preparing a quote:		
	 Information on policy & coverage: Type of cover Payment frequency Voluntary excess Details of proposer: Age & Gender Marital Status Occupation 	 Details of each driver: Driver experience Driver restrictions Age & Relationship Details of vehicle: Registration Number Make/Model Parking Location 		
Risk Factors –	Some risk factors used in motor insuran	Some risk factors used in motor insurance pricing are:		
Motor Insurance	Drivers:	Environment:		
	 Driving style, experience, level of skill, powers of observation, risk attitude, ability to predict road hazards Vehicle: Value of vehicle/repair costs if damaged Safety features available to protect passengers & theft Make, model, speed, size 	 Geography where the vehicle is used Type of road Time of the day and pedestrian risk Natural hazards Exposure: Amount of driving (miles/minute) Third Parties: Other people in the vicinity of the insured 		
Information on Proposal	An insurer would seek the following info			
Form – Home Insurance	Policy:	House Details:		
	 Date on risk Number of adults Number of claims Type of cover Accidental damage cover Excess Proposer: Age, gender, marital status Smoker/non-smoker Employment status 	 Year of purchase Type of property Building status Construction type Postcode Ownership Contents value Flood/subsidence Lock types 		
External Data	Information on Proposer:	Information on insured asset:		
	 Previous insurer claims experience Cross-product holdings Customer lifetime value models Customer behavior models Credit score Information on Location: Socio-economic data of the region Soil type data for subsidence Flood data, theft survey data 	 Data from insurers' trade body, for example ABI in the UK Data from motor registration au- thority Additional asset data Data from inter-industry agree- ment to share claims and under- 		

• Census & Valuation data

Proxy Rating Factors	factors to qua 1. The ex 2. Wheth 3. Wheth	antify risk. T extent to which er the proxy er the factor egree of ove	he effectivened a the factor d is a verifiab has a clear	ess of such pr lirectly reflec ole fact know influence or	oxy factors de ets an actual en to the proper	risk
Spatial Smoothing	Spatial smoo ducing noise			predictions ba	sed on neighb	ooring values, re-
	Distance-base	ed Smoothing				
	• C • A • U • S	Gives more we applies regard Jseful for wea imple to imp	eight to closes lless of urban ther related p lement witho	r location cod /rural status perils	tion codes bas les and less to or natural ba putional assum	rriers
	• C • Ii • A	Considers info Complex proc ncorporates d accounts for r	rmation abou ess since each listributional natural or art	assumptions	ighboring loca enced by its n aries like rivers	eighbors
Forms of Model		For different model forms like claim frequency, claim severity, propensity, etc., we use different distributions, link functions, scale parameters, etc. A summary of this is as follows:				
	Model	Error Distribu- tion	Link Function	Scale Parame- ter	Variance Function	ω_i
	Claim Frequency	Poisson	ln(y)	1	μ	Exposure
	Claim Numbers	Poisson	ln(y)	1	μ	1
	Claim Severity	Gamma	ln(y)	Estimated	μ^2	Claim Numbers
	Total Claims Cost	Tweedie	ln(y)	Estimated	$\mu^{1.5}$	Exposure
	Propensity	Binomial	$\ln\left(\frac{y}{1-y}\right)$	1	$\mu(1-\mu)$	1
Initial Analyses	Prior to mult	ivariate mode	elling, initial	analyses are	performed. Th	nis includes:
		ay analyses ay analyses			elation analys ribution analy	
One-way Analyses	One-way ana	lyses are perf	formed for the	e following re	asons:	
	2. They h	help to identif	fy levels in a	factor that h	ach factor leve ave low or no impact of a pa	

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Two-way Analyses	Two-way analyses examine key statistics across factor combinations to identific teractions between covariates. This is particularly helpful when there is some relation between variables.	•
Correlation Analyses	An understanding of the correlation between variables is helpful when interpr the results of a GLM. For categorical factors, Cramer's V statistic is used.	reting
Distribution Analyses	Distribution analysis involves examining how response distribution varies a factor levels, detecting anomalies like large claims, and identifying biases in average reserves.	
Claim Types	Different claim types must be modelled separately because they may be affected by different rating factors in different ways. This also helps in modelling prochaving different coverages.	
Model Combining	When modelling, we model frequency and severity separately. We also mode ferent claims types separately. However, all of it needs to be combined to fine ultimate cost of a claim.	
Model Validation	Models need to be validated by testing on "out-of-sample" data. Another we do this exercise is to plot a graph of predicted values and actual values from out-of-sample data to analyze the differences.	
Lift Curve	A lift curve helps assess a model's accuracy by ranking policies (in order of experience according to the model being tested) based on predicted claims grouping them into equal bands. The actual claims for each group are then plot A steeper curve means the model better separates high and low risks, making more effective. This also helps compare different models.	s and otted.
Gains Curve	The gains curve is also a way to validate a model. In this method, data is random high to low based on predicted values. The chart then compares the cumul predicted and actual values. The Gini coefficient measures the model's life represents the area between the model curve and the diagonal, showing how the model distinguishes risk levels. The higher the Gini coefficient, the more predictive the model.	lative ft—it v well
Implementing Rates	Before the theoretical premium rates from the model are implemented, they to be compared with current rates and competitors rates .	need

CREDIBILITY THEORY

Credibility Theory

Credibility theory can be used to set premium rates by considering both actual experience and external information. The basic formula for credibility-weighted estimate is:

Estimate = $Z \times (\text{Observation}) + (1 - Z) \times (\text{Other Information})$

Classical Credibility Theory

This method involves considering the quantity of data needed before we can assign 100% credibility to observed data. This is also known as "full credibility criterion." "Partial Credibility" is when we have less experience data than is needed for achieving full credibility.

The 'Bayesian' credibility, Z_B , is based on minimizing mean square error, and is **Bayesian Credibility** given by:

where

$$Z_B = \frac{n}{n+k}$$

n

$$k = \frac{E[s^2(\theta)]}{\operatorname{var}(m(\theta))}$$

Classical vs Bayesian Credibility

Standards for Full Credibility

Both methods may produce the same results if the full credibility standard for classical credibility n_N is about 7 to 8 times larger than the Bayesian credibility factor k. Bayesian credibility never reaches Z = 1. Both the models are affective at improving the stability and accuracy of estimates.

If the objective is to be within a proportion of $\pm k$ of the mean, μ , with the probability of at least P, then for $\Phi(y) = \frac{1+P}{2}$, standards for full credibility are:

Measure	Standards for Full Credibility
Frequency (Poisson)	$n_N \ge \frac{y^2}{k^2}$
Frequency (General)	$n_N \ge \frac{y^2}{k^2} \left(\frac{\sigma_N^2}{\mu_N}\right)$
Severity	$n_X \ge \frac{y^2}{k^2} \left(\frac{\sigma_X}{\mu_X}\right)^2$
Aggregate Losses (Poisson)	$n_S \ge n_N + n_X$
Aggregate Losses (General)	$n_S \ge \left(\frac{y}{k}\right)^2 \left(\frac{\sigma_N^2}{\mu_N} + \frac{\sigma_X^2}{\mu_X^2}\right)$

Partial Credibility

Square Root Rule – If n is the expected number of claims for the volume of data, and n_N is the standard for full credibility, the partial credibility is:

$$Z = \sqrt{\frac{n}{n_N}}$$

Buhlmann-Straub Credibility Model

•

- V_i = Volume Measure for risk i
- $S_i =$ Insurance claims for risk i
- $X_i = \text{claims ratio} = \frac{S_i}{V_i}$ for risk *i*

The model assumes the existence of a latent parameter θ_i such that:

$$E[X_{ik} \mid \theta_i] = \mu(\theta_i),$$

$$Var[X_{ik} \mid \theta_i] = \frac{\sigma^2(\theta_i)}{V_{ik}}.$$

The benchmark claims ratio is: $\beta = E[\mu(\theta_i)]$

The expected variance of the observed claims ratio per unit of V is: $\phi = E[\sigma^2(\theta_i)]$ The Variance of the long-run claims ratio for all risks is: $\lambda = \operatorname{var}[\mu(\theta_i)]$ The credibility-based claims ratio is: $C = z_i X_i + (1 - z_i)\beta$ where $z_i = \frac{V_i}{V_i + \frac{\beta}{2}}$

The following are the assumptions of Buhlmann-Straub credibility model:

- 1. V_i and X_i are based on volume measures V_{ik} and claims ratio X_{ik} for risk i across years k
- 2. The *i*-th risk is described by pair, $(\theta_i, (X_{ik})_{k\geq 1})$ where $(X_{ik})_{k\geq 1}$ is the sequence of claims ratios observed for risk *i*
- 3. The çairs $(\theta_i, (X_{ik})_{k>1})$ are mutually independent
- 4. The θ_i are independent and identically distributed
- 5. Conditionally on θ_i , the X_{ik} are independent

An actuary must consider the following issues when choosing the complement:

- Competitive market issues
 - Statistical issues
 - Practical issues

Assumptions of Buhlmann-Straub Credibility Model

Complement of Credibility

• Regulatory issues

Desirable Qualities of Complement of Credibility

Practical Issues when using Credibility Theory

The desirable qualities of the complement of credibility are:

- accuracy as a predictor of next year's mean loss costs
- unbiasedness as a predictor of next year's mean loss costs
- independence from the base statistic
- availability of data
- ease of computation
- relationship to loss costs

Issues to consider when using credibility theory are:

- 1. simplicity
- 2. visibility imposing a maximum swing, or self-rating
- 3. goodness of fit (accuracy vs. simplicity)
- 4. level of grouping vs. accuracy
- 5. source of data
- 6. stability of data
- 7. use of partial premiums
- 8. choice of complement of credibility
- 9. judgement when considering how to allow for large claims

REINSURANCE PRICING

Similarity – Direct and Reinsurance Pricing	 The underlying principles of deriving the risk premium and office premium are the same for the reinsurance business as for the direct business. The office premium would be estimated after allowing for: <u>Expenses</u> – A reinsurer would load for its own expenses using the same techniques as an insurer. <u>Profit/ROE</u> – As insurers, reinsurers would also build a profit loading. <u>Brokerage and Commission</u> – For Quota Shares, reinsurance premiums are higher so the brokerage is lower (in the range of 1%-2%). 	
Differences – Direct and Reinsurance Pricing	 The differences between direct and reinsurance pricing are: 1. the volume and data available will be different 2. there are very few standard contracts 3. the individual nature of the pricing exercise 4. reinsurance pricing may be stochastic 5. pricing depends on whether the reinsurer is required to quote 6. the cedant is as knowledgeable as the reinsurer, which is not the case between insurer and policyholder in direct insurance 7. the exact pricing approach also differs materially by line of business 	
Proprietary Catastrophe Models	 Proprietary CAT models like RMS, AIR and EQECAT are used to price property cat business. When comparing models, it is important to consider: different models are better suited for different perils different models use different assumptions Input data needs vary by model which influences reliability the output from different models may differ 	
Occurrence Exceedance Probability	The probability that the largest individual event loss in a year exceeds a particular threshold.	
Aggregate Exceedance Probability	The probability that the aggregate losses from all risk events in a year exceeds a particular threshold.	

Non-Proportional Reinsurance In exposure rating, reinsurers would rely on benchmarks to represent the market

Pricing – Exposure Rating	severity distribution. Suppose an excess of loss reinsurance treaty layer LR xs ER . The 100% limit is L and policy excess is E . Then, the proportion of premium to be allocated to the given layer is given by:
	$\mathbf{Proportion} = \frac{ILF(LR + ER) - ILF(ER)}{ILF(L + E) - ILF(E)}$
	The above formula may need adjustments for:
	 when the reinsurance retention is below the bottom of the cover on risk, ILF(ER) is replaced with ILF(E) when the top of the reinsured layer is beyond the top of the cover on risk, ILF(ER+LR) becomes ILF(E+L) when the reinsurance layer finishes below the risk (0% reinsured) when the reinsurance layer starts above the cover on risk (0% reinsured)
	Practical considerations in exposure rating –
	 Reinsurers might have limited historical loss data Pricing of high excess layers reinsurance is derived by minimum rate requirement In some cases, the cedant does not provide individual risk information When this happens, the reinsurer needs to make a judgement on where in the interval the limit actually lies.
Non-Proportional Reinsurance Pricing – Experience Rating	We may use the following approaches for experience rating:1. Burning cost method2. Frequency-severity method
Burning Cost Approach	The common steps involved in pricing a non-proportional reinsurance treaty using the burning cost approach are:
	 The reinsurer first applies trends to historical loss data. The format of this data depends on the type of cover (LOD/RAD) The loss data from the insurer must be from ground-up and uncapped. Trends would be applied to past paid claims and case reserves. Then, reinsurance terms would be applied to the trended losses Trended losses to be used to fit statistical methods to find the ultimate If data is limited, benchmark data is used Now, consider the relevant exposure measure i.e., premium/SI Historical premiums to be adjusted to find 'as-if' premiums The exposure measure also needs to be adjusted for inflation We bring losses and exposure on a common level Estimate the loss costs by averaging losses to the layer for all years or estimating lost cost rate for all years and then averaging them. We then need to estimate any trends in the loss cost The final loss cost rate to be determined with underwriters
Frequency Severity Approach	This method involves the following steps:
	 Losses are adjusted for trends Development for open claims in recent years to be considered Applying aggregate development factors to individual claims might understate variability IBNER to be estimated for open, non-settled claims Large loss count development may be used to estimate IBNR Frequency & Severity distributions to be combined

6. Frequency & Severity distributions to be combined

SP8 Summary Sheet

Practical Issues in Non-Proportional Reinsurance Pricing	 The following practical issues may arise in non-proportional reinsurance pricing: Reporting threshold for large loss data Choice of inflation rates Treatment of shock losses Discounting of future loss costs Changes in cedant business mix 			
Proportional Reinsurance Pricing	 In proportional reinsurance pricing, the task is not to find the premium rate, but rather to: Assess the likely overall loss ratio Determine the level of ceding/ profit commission that may be offered 			
Assessment of Overall Loss Ratio	 The steps involved in assessing overall loss ratio include: Collecting Data Projecting ultimate claims for each year and calculating loss ratios Applying trends to the loss ratios to reflect the upcoming period Making an estimate of the overall loss ratio based on various methods 			
Determining the level of ceding/profit commission	If the ceding commission is flat and there is no profit commission, the reinsurer would check if $100 - loss ratio\% - ceding commission\%$			
	leaves enough for profits and other expenses of the reinsurer. When there is a sliding scale ceding commission or a profit commission with a flat ceding commission, the loss ratio distribution would be needed to estimate the reinsurer's financial position distribution.			
Surplus Share Reinsurance Pricing	Surplus share contracts may be modelled similar to Quota Share treaties. However, an important complication is that the loss ratio or claims experience might be different for the insurer and reinsurer. The reinsurer's experience is dependent on the way in which large losses are distributed. Risks with higher limits, and therefore higher cession rates, will have much larger losses than those with lower cession. Here, the ceded loss ratio is higher than the original loss ratio. The opposite of this is also true. The reinsurer, therefore, needs to be confident about:			
	Large limit risks not having disproportionately heavy large loss experienceContracts terms restricting choices a cedant makes about the amount ceded			
	The risk data, therefore, needs to be used to assess the likely distribution of cession rates.			
Stop Loss Reinsurance Pricing	Stop Loss reinsurance is priced in a similar way to an excess of loss reinsurance, except that loss ratios are used as attachment and detachment points rather than monetary amounts.			
Pricing other features of Reinsurance Contract	 While pricing a reinsurance treaty, certain complicated and unusual features of the treaty need to be adjusted for. Examples of a few are: Reinstatement Premiums Aggregate deductibles Indexation clauses Swing Rates Loss Ratio Caps 			

CATASTROPHE MODELS

Catastrophe v/s Traditional Models	Traditional pricing methods like Frequency-Severity and Burning Cost method work well for high-frequency, low-severity risks but not for low-frequency high- severity risks . The reason being that past loss data may be too limited to reflect the true risk, because the return period of losses is much longer than the ob- servation period. CAT models estimate losses based on the insured's geographical locations.
Structure of Catastrophe Models	All catastrophe models follow a same generic structure, consisting of the following interlinked modules:
	$\underline{\text{Event Module}}$ – This module is a database of stochastic events.
	<u>Hazard Module</u> – This module consists of the hazard of each event.
	$\underline{ \mbox{Inventory Module} - \mbox{This module consists of all details regarding insured's risks and associated risk factors.}$
	$\frac{\text{Vulnerability Module}}{\text{is likely to sustain from a peril.}}$
	$\label{eq:main} \underbrace{ \mbox{Financial Analysis Module}_{\mbox{excess, coverage terms, etc.}} \mbox{ - This module consists of policy conditions like limits, } \\$
Key Perils Modelled	Common perils modelled in catastrophe models are: Hurricane Earthquake Tornadoes Hailstorms Winter storms Floods

- Diseases
- Non-natural perils